

**PAPER : JNU 2012**  
**PHYSICS-PH**

**OBJECTIVE QUESTIONS**

1. The general solution of the differential equation,  $x^2 \frac{d^2 y}{dx^2} - 2x \frac{dy}{dx} + 2y = 0$  in terms of two arbitrary constants A and B, is

(a)  $e^{1/x} \left( A \cos\left(\frac{1}{x}\right) + B \sin\left(\frac{1}{x}\right) \right)$

(b)  $Ax + \frac{B}{x}$

(c)  $Ax + Bxe^x$

(d)  $Ax + Bx^2$

2. If  $a, b$  and  $c$  are non-zero real numbers not equal to 1,  $\log_a c$  can be expressed as

(a)  $\log_b c / \log_b a$

(b)  $\log_b a / \log_b c$

(c)  $\log_c a / \log_b a$

(d)  $\log_c b / \log_a b$

3. A homogeneous linear transformation takes the point (1, 1) in the xy-plane to the point (3, 3) and keeps the point (1, -1) fixed (i.e., it remains (1, -1) after the transformation). The matrix corresponding to this transformation is

(a)  $\begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix}$

(b)  $\begin{pmatrix} 3 & 0 \\ 0 & 2 \end{pmatrix}$

(c)  $\begin{pmatrix} 2 & 1 \\ 1 & 2 \end{pmatrix}$

(d)  $\begin{pmatrix} 2 & -1 \\ -1 & 2 \end{pmatrix}$

4. The function  $\frac{1}{\cosh x}$  may be expressed around the point  $x = 0$  as a power series as

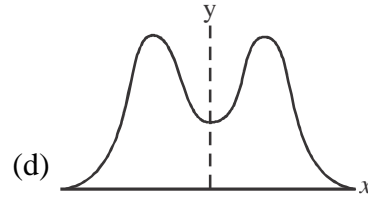
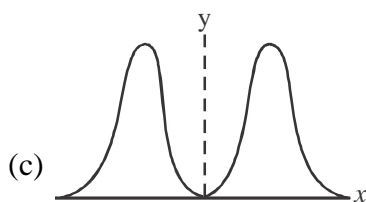
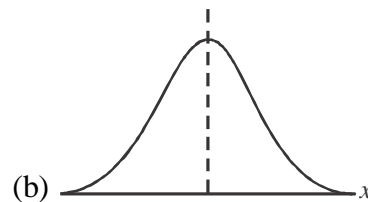
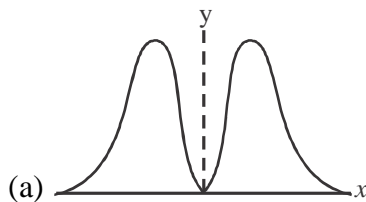
(a)  $1 - \frac{1}{2}x^2 + \frac{1}{24}x^4 - \frac{1}{720}x^6 + \dots$

(b)  $1 - \frac{1}{2}x^2 + \frac{5}{24}x^4 - \frac{61}{720}x^6 + \dots$

(c)  $1 - \frac{1}{2}x^2 + \frac{11}{24}x^4 - \frac{331}{720}x^6 + \dots$

(d)  $1 - \frac{1}{2x^2} + \frac{1}{24x^4} - \frac{1}{720x^6} + \dots$

5. Which of the following graphs gives the best representation of the real-valued function  $y = x^2 e^{-x^2}$  ?



6. An observer O uses the coordinate system  $(x, t)$  to describe non-relativistic motion in one dimension. Another observer O', moving with respect to O with a uniform velocity 'v' (much smaller than the speed of light c) along the positive x-direction, uses  $(x', t')$ , such that at  $t = 0, t' = 0$  and that instant x and x' coincide. then

(a)  $x' = x - vt, t' = t, \frac{\partial}{\partial x'} = \frac{\partial}{\partial x} - \frac{1}{v} \frac{\partial}{\partial t}$  and  $\frac{\partial}{\partial t'} = \frac{\partial}{\partial t}$

(b)  $x' = x - vt, t' = t, \frac{\partial}{\partial x'} = \frac{\partial}{\partial x}$  and  $\frac{\partial}{\partial t'} = \frac{\partial}{\partial t} + v \frac{\partial}{\partial x}$

(c)  $x' = x + vt, t' = t, \frac{\partial}{\partial x'} = \frac{\partial}{\partial x} + \frac{1}{v} \frac{\partial}{\partial t}$  and  $\frac{\partial}{\partial t'} = \frac{\partial}{\partial t}$

(d)  $x' = x + vt, t' = t, \frac{\partial}{\partial x'} = \frac{\partial}{\partial x}$  and  $\frac{\partial}{\partial t'} = \frac{\partial}{\partial t} - v \frac{\partial}{\partial x}$

7. A ball dropped from a height h can only attain the height  $4h/5$  after bouncing off the floor. If the ball is dropped from a height of 1 m, the time it will take to come to rest is, approximately  
[ Ignore air resistance and the finite radius of the ball. ]

(a) 1.9 s                      (b) 3.8 s                      (c) 8.0 s                      (d) 4.1 s

8. A small raindrop of mass m experiences a viscous drag force  $F_d = bv$ , proportional to its instantaneous speed 'v'. If it starts from rest at a height h, its speed after a time 't' is

(a)  $v(t) = \frac{mg}{b} \tanh\left(\frac{bt}{m}\right)$                       (b)  $v(t) = \frac{mg}{b} e^{-bt/m}$

(c)  $v(t) = \frac{mg}{2b} (1 - e^{-2bt/m})$                       (d)  $v(t) = \frac{mg}{b} (1 - e^{-bt/m})$

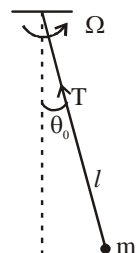
9. The nature of flow in a viscous liquid is characterised by the dimensionless Reynolds' number Re proportional to  $v$  (the flow velocity) :  $Re \propto v$ . Given that Re also depends on (i) the density  $\rho$  of the fluid, (ii) the dynamical viscosity  $\eta$  and (iii) a characteristic length  $l$ , of the flow. By dimensional analysis, we find that

(a)  $Re = \frac{\eta \omega}{\rho}$                       (b)  $Re = \frac{\rho \omega}{\eta}$                       (c)  $Re = \frac{\rho \eta v}{l}$                       (d)  $Re = \frac{\rho v}{\eta l}$

10. A ball of mass m is hung from a support by a massless wire of length  $l$ . The support is rotated with an angular speed.  $\Omega > \sqrt{g/l}$  around a vertical axis through the point of suspension as shown in the figure. The ball rests in equilibrium at an angle  $\theta_0$ . Which the following statements concerning  $\theta_0$  and the tension T, is true ?

(a)  $\theta_0 = 0$  and  $T = mg$                       (b)  $\theta_0 = \tan^{-1}\left(\frac{g}{\Omega^2 l}\right)$  and  $T < mg \cos \theta_0$

(c)  $\theta_0 = \sin^{-1}\left(\frac{g}{\Omega^2 l}\right)$  and  $T > mg \cos \theta_0$                       (d)  $\theta_0 = \cos^{-1}\left(\frac{g}{\Omega^2 l}\right)$  and  $T > mg \cos \theta_0$



11. In a wire loop of resistance  $R$  and inductance  $L$ , an e.m.f.  $\varepsilon$  is switched on at  $t = 0$ . The magnetic flux through the loop is given by

- (a)  $\frac{L\varepsilon}{R}(1 - e^{-tR/L})$       (b)  $\frac{L\varepsilon}{R}e^{-tR/L}$       (c)  $\frac{L\varepsilon}{R}\left(1 - \frac{L}{tR}\right)$       (d)  $\frac{L\varepsilon}{R}$

12. The electric and magnetic fields of an electromagnetic wave in vacuum are given by

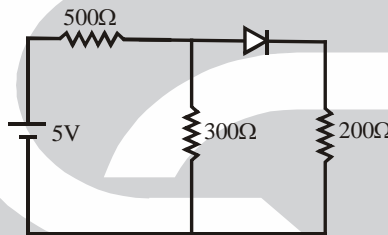
$\mathbf{E} = \hat{i}E_0 \sin(kz - \omega t)$  and  $\mathbf{B} = \hat{j}B_0 \sin(kz - \omega t)$  respectively. Which of the following relations is correct ?

- (a)  $k^2E_0 = \omega^2B_0$       (b)  $\omega E_0 = kB_0$       (c)  $kE_0 = \omega B_0$       (d)  $E_0B_0 = \omega k$

13. The radius of the nucleus of the Ra atom, which carries an electric charge  $+88e$ , is  $7.0 \times 10^{-15}$  m. What should roughly be the speed of a proton, if it has to reach as close as  $1.0 \times 10^{-14}$  m from the centre of the nucleus? [The radius of the cloud of orbital electrons of the Ra atom is approximately  $5.0 \times 10^{-11}$  m.]

- (a)  $6.7 \times 10^9$  m/s      (b)  $3.1 \times 10^8$  m/s      (c)  $1.4 \times 10^5$  m/s      (d)  $4.9 \times 10^7$  m/s

14. In the circuit shown below, the diode is non-ideal and has a voltage drop of 0.7 V. What is the value of the diode current ?

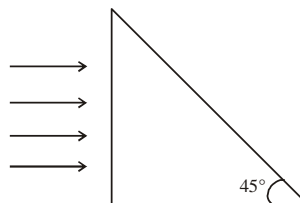


- (a) 4.84 mA      (b) 8.06 mA      (c) 3.03 mA      (d) 6.25 mA

15. The Doppler width  $\Delta\lambda$  of the orange line (for which  $\lambda = 6058 \text{ \AA}$ ) of Kr is  $0.0055 \text{ \AA}$ . What is the spread in frequency of this spectral line?

- (a)  $2.7 \times 10^7$  Hz      (b)  $2.7 \times 10^9$  Hz      (c)  $4.5 \times 10^6$  Hz      (d)  $4.5 \times 10^8$  Hz

16. A beam of light, consisting of red (R), green (G) and blue (B) colours, is incident normal to a face on a right-angled prism (see figure). The refractive indices of the material of the prism for R, G and B wavelengths are 1.39, 1.44 and 1.47 respectively. Then



(a) R, G and B get transmitted (without undergoing total internal reflection)

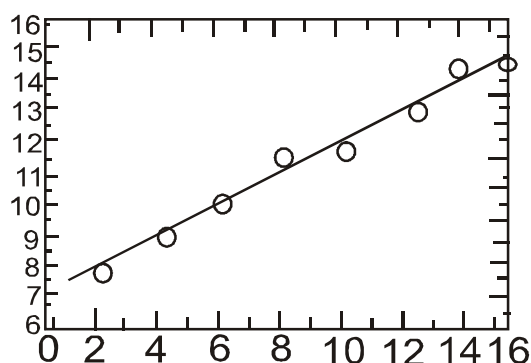
(b) R and G undergo total internal reflection and B gets transmitted

(c) R gets transmitted, while G and B undergo total internal reflection

(d) All of R, G and B undergo total internal reflection

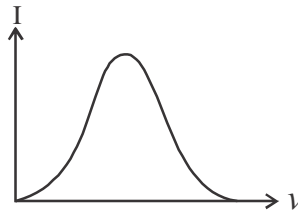


24. The ratio of the specific heat capacity and temperature,  $C_v/T$ , of Cu is plotted as a function of  $T^2$ , the square of the absolute temperature, in the graph below:



The values of  $\gamma$  and  $\beta$  (the coefficients corresponding to the electronic and the vibrational components of the specific heat) are, approximately

- (a)  $\gamma = 7.0 \times 10^{-4} \text{ J mol}^{-1} \text{ K}^{-2}$  and  $\beta = 5.0 \times 10^{-5} \text{ J mol}^{-1} \text{ k}^{-4}$   
 (b)  $\gamma = 5.0 \times 10^{-5} \text{ J mol}^{-1} \text{ k}^{-2}$  and  $\beta = 7.0 \times 10^{-4} \text{ J mol}^{-1} \text{ k}^{-4}$   
 (c)  $\gamma = 1.4 \times 10^{-3} \text{ J mol}^{-1} \text{ k}^{-2}$  and  $\beta = 7.0 \times 10^{-4} \text{ J mol}^{-1} \text{ k}^{-4}$   
 (d)  $\gamma = 5.0 \times 10^{-4} \text{ J mol}^{-1} \text{ k}^{-2}$  and  $\beta = 7.0 \times 10^{-5} \text{ J mol}^{-1} \text{ k}^{-4}$
25. A paramagnetic gas at room temperature is placed in an external magnetic field of 1.5 T (tesla). Each atom of the gas has a magnetic moment  $\mu = 1.0 \mu_B$ , where  $\mu_B = 9.3 \times 10^{-24} \text{ J/T}$  is the Bohr magneton. The difference in energy when an atom is aligned along the magnetic field and opposite to it, is  
 (a)  $2.8 \times 10^{-23} \text{ J}$       (b)  $1.4 \times 10^{-23} \text{ J}$       (c)  $18.6 \times 10^{-24} \text{ J}$       (d)  $9.3 \times 10^{-24} \text{ J}$
26. The Fermi energy  $\epsilon_F$  in metals depends on the number density  $n_e$  of mobile electrons, which may be thought of as a free Fermi gas. If  $n_e$  of one metal is larger by a factor of 1000 compared to another, then in comparison, its Fermi energy is  
 (a) 1000 times larger      (b) smaller by a factor of 1/100  
 (c) 100 times larger      (d) 10 times larger
27. The kinetic energy of a proton and an  $\alpha$ -particle (not under the influence of any force) are given to be equal. If we denote the de Broglie wavelengths of the proton by  $\lambda_p$  and that of the  $\alpha$ -particle by  $\lambda_\alpha$ , then  
 (a)  $\lambda_p \approx \lambda_\alpha$       (b)  $\lambda_p \approx 4\lambda_\alpha$       (c)  $\lambda_p \approx \frac{1}{2}\lambda_\alpha$       (d)  $\lambda_p \approx 2\lambda_\alpha$
28. When a monochromatic point source of light is placed at a distance of 0.2 m from a photoelectric cell, the stopping potential  $V_s$  and the saturation current  $I_s$  are found to be 0.6 V and 18.0 mA, respectively. If the same source is now placed 0.6 m away from the photoelectric cell, one finds  
 (a)  $V_s = 0.2 \text{ V}$  and  $I_s = 6.0 \text{ mA}$       (b)  $V_s = 0.6 \text{ V}$  and  $I_s = 6.0 \text{ mA}$   
 (c)  $V_s = 0.6 \text{ V}$  and  $I_s = 2.0 \text{ mA}$       (d)  $V_s = 0.2 \text{ V}$  and  $I_s = 18.0 \text{ mA}$
29. The graph in the figure below shows the intensity  $I$  as a function of frequency  $\nu$  of a perfect blackbody at a fixed temperature  $T$ :



The corresponding graph at temperature  $2T$  can be obtained by which of the following operations ?  
For every point of the graph

- (a) multiply the  $\nu$ -coordinate by  $1/2$  and the  $I$ -coordinate by 8  
 (b) multiply the  $\nu$ -coordinate by 2 and the  $I$ -coordinate by 8  
 (c) multiply the  $\nu$ -coordinate by  $1/2$  and the  $I$ -coordinate by 16  
 (d) multiply the  $\nu$ -coordinate by 2 and the  $I$ -coordinate by 16

30. What is the maximum theoretical accuracy  $\Delta E$  to which an ideal experiment may determine the energy levels of the hydrogen atom ?

[Hint : Use the fact that the age of the universe is estimated to be approximately  $1.4 \times 10^{10}$  years.]

- (a)  $4.7 \times 10^{-26}$  eV      (b)  $9.4 \times 10^{-33}$  eV      (c)  $1.2 \times 10^{-63}$  eV      (d)  $2.4 \times 10^{-70}$  eV

31. A particle in one dimension is in the ground state (lowest energy quantum state) of the potential well given by

$$V(x) \begin{cases} 0 & \text{for } |x| < \frac{L}{2} \\ \infty & \text{otherwise} \end{cases}$$

Let  $P_+$  be the probability that the particle is found to move along the positive  $x$ -direction and  $p$  be the magnitude of the momentum for that state of motion. Then

- (a)  $P_+ = 0$  and  $p = 0$       (b)  $P_+ = \frac{1}{2}$  and  $p = \frac{\pi}{2L}$       (c)  $P_+ = \frac{1}{2}$  and  $p = \frac{\pi}{L}$       (d)  $P_+ = 1$  and  $p = \frac{\pi}{L}$

32. A particle of mass  $m$  is moving in a three-dimensional potential

$$V(x, y, z) = \frac{1}{2} m \omega^2 (x^2 + 2y^2 + 4z^2)$$

The energy of the particle in the ground state (lowest energy quantum state) is

- (a)  $\frac{\sqrt{7}}{2} \hbar \omega$       (b)  $\frac{3}{2} \hbar \omega$       (c)  $\frac{7}{2} \hbar \omega$       (d)  $\frac{(3 + \sqrt{2})}{2} \hbar \omega$

33. A nucleus may be modelled as a drop of liquid consisting of the nucleons (protons and neutrons). In this model, the dominant contribution to the nuclear binding energy is from the volume, which is proportional to  $A$ , the total number of nucleons. Then the two important subdominant contributions from the surface tension and the coulomb repulsion of the protons are, proportional to

- (a)  $A^{2/3}$  and  $Z / A^{1/3}$  respectively      (b)  $A^{2/3}$  and  $Z^2 / A^{1/3}$  respectively  
 (c)  $A^{1/3}$  and  $Z^2 / A^{2/3}$  respectively      (D)  $A^{1/2}$  and  $Z^2 / A^{1/3}$  respectively